Gauge R & R

Evaluating the Precision of your Measurement System

Precision Scientific Software Inc.

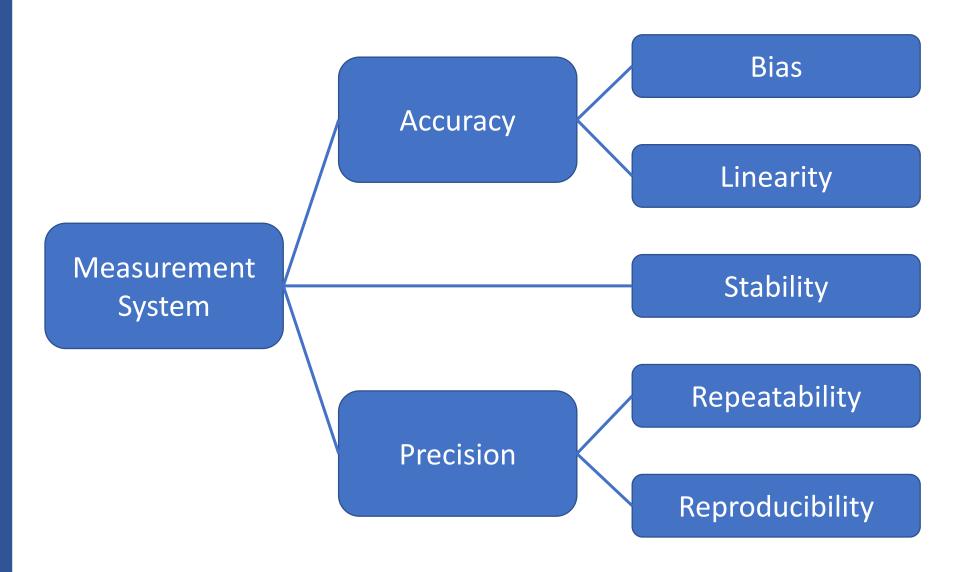
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Measurement System Analysis (MSA)

- Variation is inherent in all measurements
 - Product and Process: input materials, production process
 - Measurement System: test methods, equipment, appraisers
- Measurement system analysis is used to analyze the contribution of the measurement system to the total variation seen in the final product
- Goal of measurement system analysis
 - Minimize the amount of variation due to the measurement system
- Variation in the measurement system should be small compared to the variation in the product
 - Ideally no more than 10% of the variation in the product and process

Components of Measurement System Variation



Components of MS Variation – Accuracy vs Precision

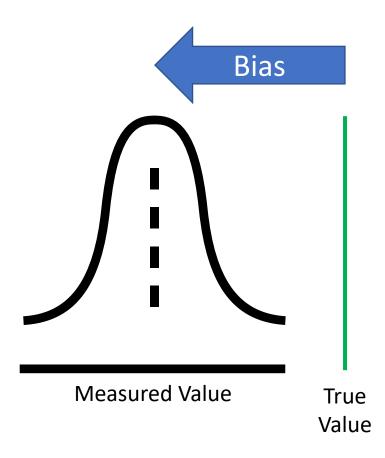
- Accuracy degree of closeness of a measurement to the true value
- Precision degree of closeness of repeated measurements to each other

Accurate and Precise	Accurate but Not Precise	Precise but Not Accurate	Not Accurate and Not Precise

- Error in Accuracy results in an error of location
- Error in Precision results in an error of spread

Components of MS Variation – Bias

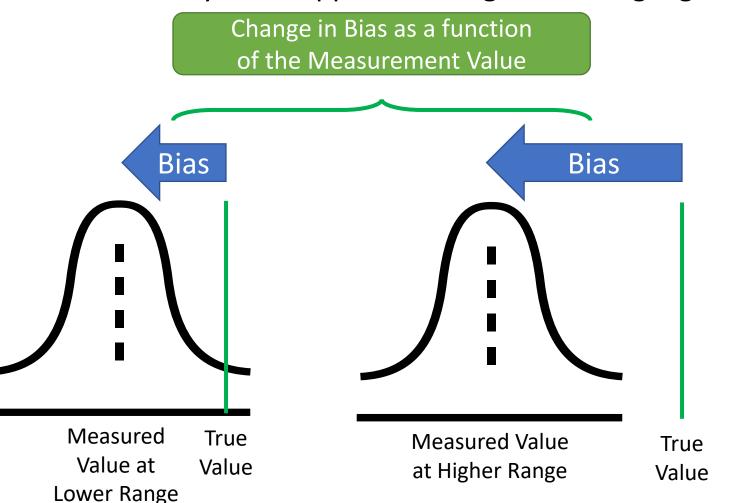
- Bias is the difference between the measured value and the true value
 - The true value can be determined by averaging repeated measurements using a "higher order" measurement device

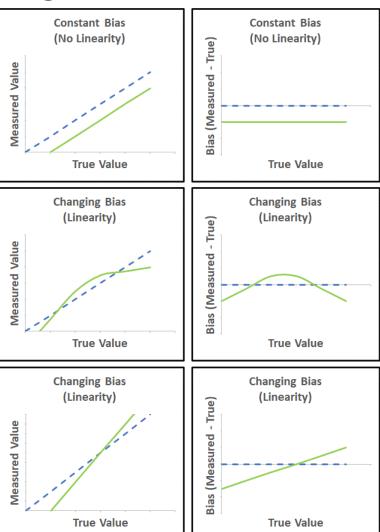


Components of MS Variation – Linearity

Linearity is the change in bias over the operating range of the instrument

Measured by same appraiser using the same gauge



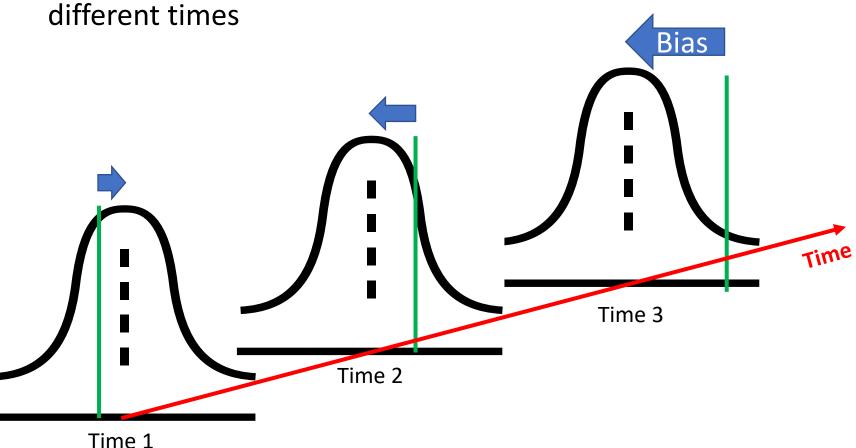


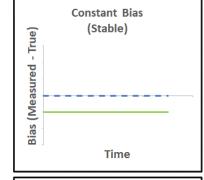
Components of MS Variation – Stability

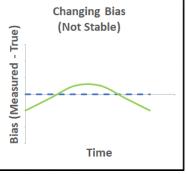
• Stability is the change in bias when measurements are made over an

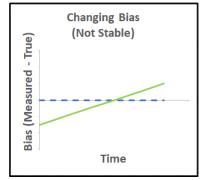
extended period of time (days / weeks / months)

• Same part measured by same appraiser using the same gauge at



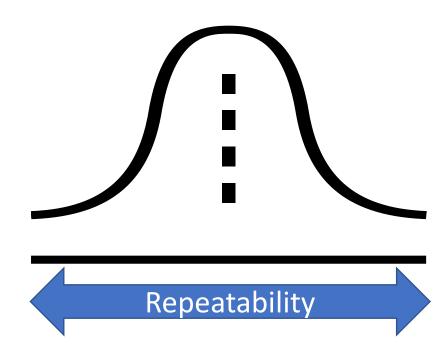






Components of MS Variation – Repeatability

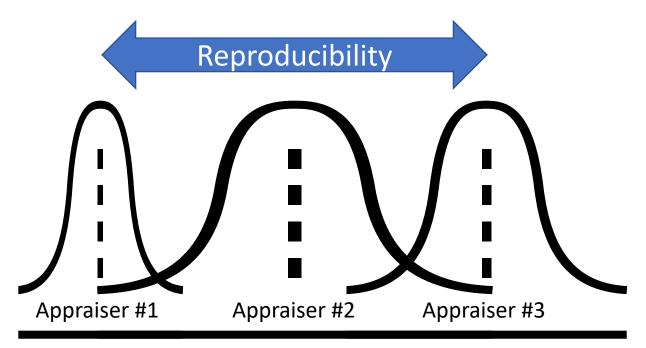
- Repeatability is amount of variation between repeated measurements
 - Same part measured by same appraiser using the same gauge at the same time
- Referred to as Equipment Variation (EV)
 - Also referred to as "within appraiser variation"



Narrower range indicates improved repeatability

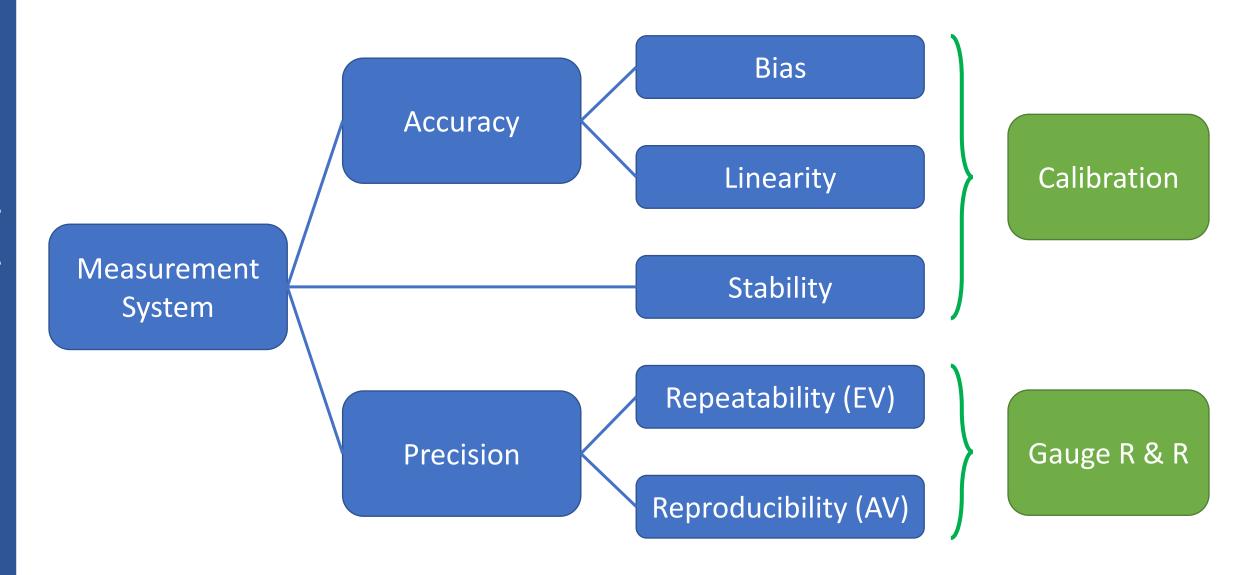
Components of MS Variation – Reproducibility

- Reproducibility is amount of variation between different appraisers
 - Same part measured by different appraisers using the same gauge
- Referred to as Appraiser Variation (AV)
 - Also referred to as "between appraiser variation"



Narrower range indicates improved reproducibility

Components of Measurement System Variation



Gauge R & R Concepts

- Measurement variation is comprised of
 - True product variation (PV)
 - Repeatability: variation due to measurement equipment (EV)
 - Reproducibility: variation due to different appraisers (AV)
- Relationship of the variances

•
$$\sigma_m^2 = \sigma_P^2 + \sigma_E^2 + \sigma_A^2$$

• Gauge R & R isolates the σ_E^2 and σ_A^2 terms to quantify the amount of measurement variation that is attributable to the measurement system

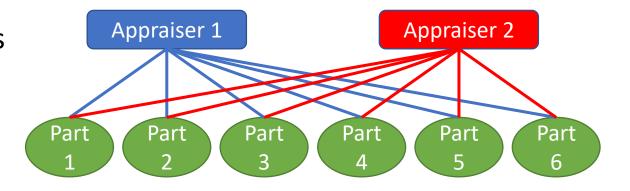
Number of observations

 Appraisers 	minimum 2	preferably 3 or 4
Parts	10	cover entire range of the product's tolerance
Trials	minimum 2	preferably 3 repeats per part per appraiser
 Observations 	$3 \times 10 \times 3 = 90$	(3 Appraisers x 10 Parts x 3 Trials)

- Parts should be presented to the appraisers in random order and masked to avoid introducing bias into the measurements
- All appraisers should use the same testing method and the same gauge
- This configuration analyzes the R & R of different appraisers
 - To analyze the R & R of different gauges, conduct the analysis with 1 appraiser using 3 gauges (randomizing the order of both the parts and the gauges)

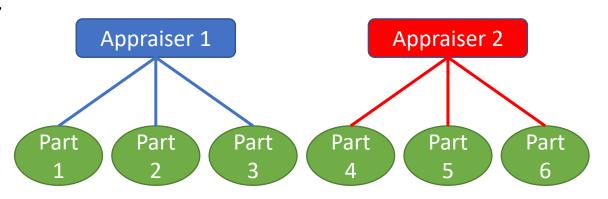
Crossed Study

- Each part measured by all appraisers
- Used for non-destructive testing
- 2-factors: appraiser and part



Nested Study

- Each part measured by one appraiser
- Used for destructive testing
- 2-factors: appraiser and part
- Care must be taken to ensure that the parts measured by each appraiser are as identical as possible



• Parts 1 & 4 should be equivalent, parts 2 & 5 should be equivalent, etc

- Destructive testing
 - There are situations where an individual part cannot be tested more than one
 - Example: testing a part either destroys or permanently changes the part
 - Collect parts from Lots which cover the entire range of the production process
 - Take individual parts from each of the Lots
 - The individual parts from each Lot should be as identical as possible
 - For instance, taking 9 individual parts from each of 10 Lots allows 3 appraisers to each test 3 parts from each of the 10 Lots
 - This design mimics a Gauge R & R Study done with non-destructive testing
 - However, there will unavoidably be a component of process variation built into the part-to-part variation (PV)
 - If the Lots are as dissimilar from each other as possible, and the parts within each Lot are as similar as possible then the degree of process variation will be minimized relative to the part-to-part variation

Standard Gauge R & R (Crossed or Nested)

- Expanded Study
 - Analyze up to 8 factors
 - Appraiser, Part,
 - Gauge, Lab, Location
 - Analyze interactions between all factors
 - Can handle missing data

 Data collection plan is often adjusted to avoid the large number of tests that would be required by repeating the standard plan for each new factor

- Example:
 - 3 appraisers use 3 gauges to measure 5 parts 2 times
 - $3 \times 3 \times 5 \times 2 = 90$ total observations

Gauge Variation
(Repeatability)

Appraiser Variation
(Reproducibility)

Appraiser vs Appraiser

Appraiser vs Part

Extended Gauge R & R

Gauge Variation (Repeatability) (Reproducibility)

Gauge vs Gauge

Gauge vs Part

Within Gauge

(Reproducibility)

Appraiser vs Appraiser

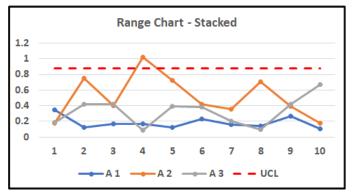
Appraiser vs Part

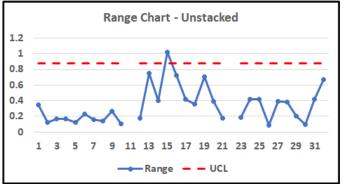
Appraiser vs Gauge

Within Appraiser

Gauge R & R Findings

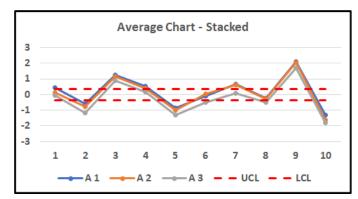
- Calculation methods
 - Range method
 - Quick approximation of measurement variability

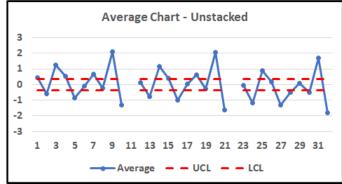




Does not compute repeatability and reproducibility separately

- Average and range method
 - Quantifies variability
 - Calculates repeatability, reproducibility, and part variation





Can only be used with Crossed Study

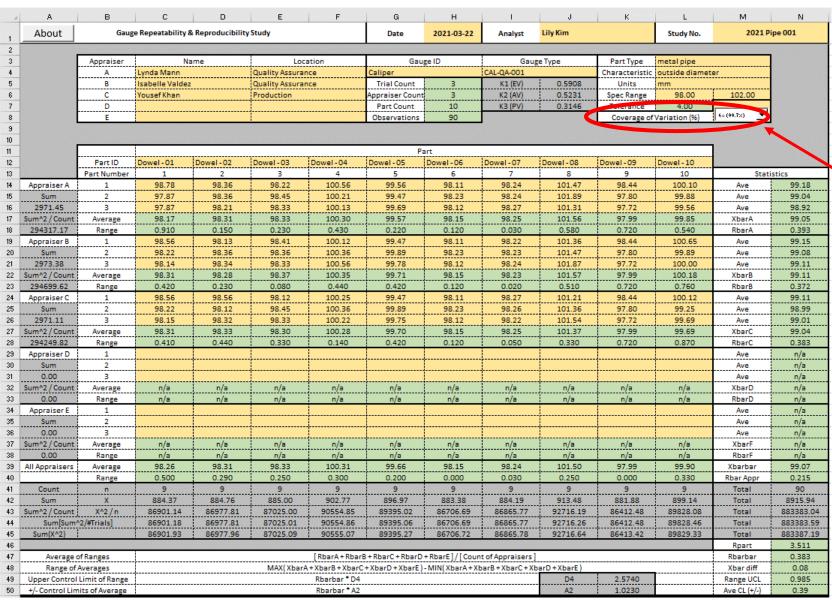
Gauge R & R Findings

- Calculation methods
 - Analysis of Variance (ANOVA) method
 - Most widely used and accurate method
 - Calculates repeatability, reproducibility, and interactions between all factors
 - Can be used with Nested, Crossed, and Extended Study types
- Targets indicating that the GRR Study was well designed and that the measurement system is suitable for the process being measured

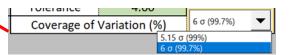
% Contribution to Variance	% of Study Variation – or – % of Process Tolerance	Comment
< 1%	< 10%	Measurement System is considered acceptable
>= 1% & < 9%	>= 10% & < 30%	Measurement System may be acceptable depending on application and cost factors, but try to improve it
>= 9%	>= 30%	Measurement System is considered unacceptable

- Number of Distinct Categories (NDC)
 - >= 5

Using the Gauge R & R Template - Data Region



Enter Study Information, including High and Low Tolerance Specs and Coverage of Variation (5.15 or 6 σ), in this top region



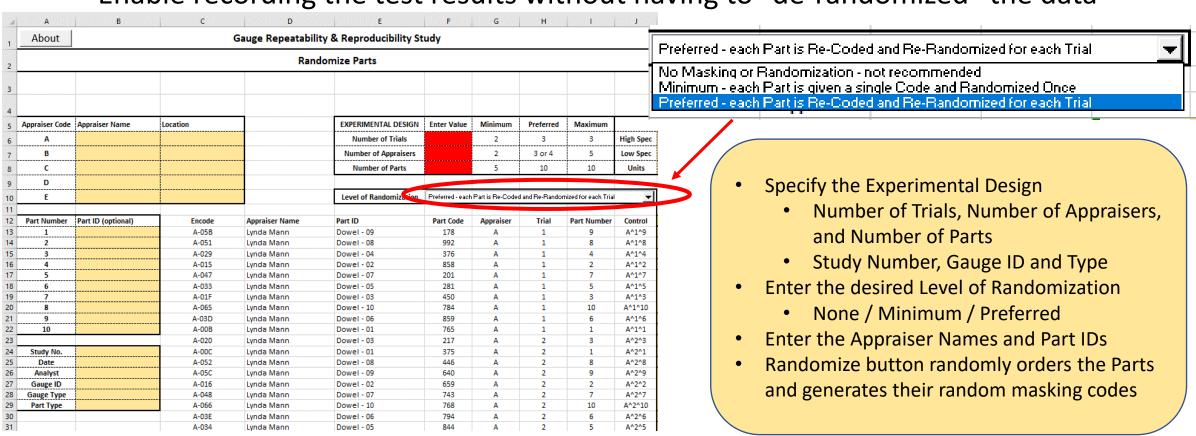
Enter the Test Results in this region. This example shows 3 Appraisers each testing 10 Parts with 3 repetitions per Part. Up to 5 Appraisers can be included in the GRR Study.

Cells are colour-coded based on their contents:

- Yellow cells: data entry
- Green cells: calculated results
- Grey cells: sub-calculations required for statistical results

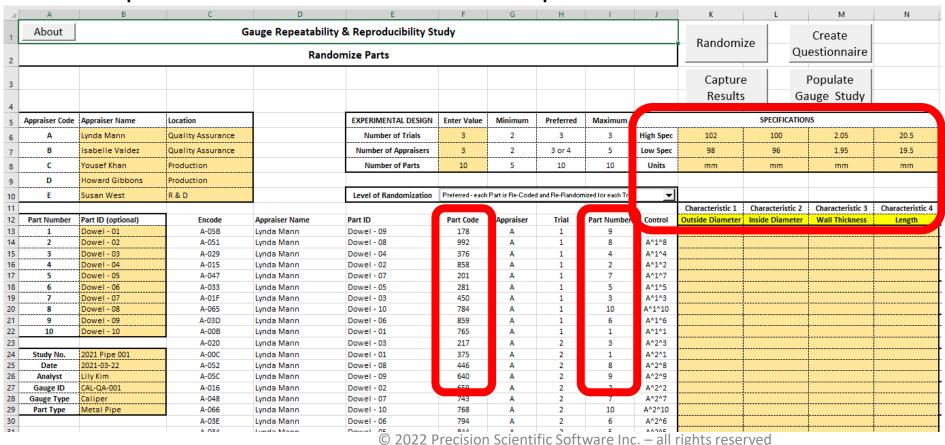
Using the Gauge R & R Template — Randomization

- The Randomize worksheet conveniently:
 - Randomize the order of presentation of the Parts to the Appraisers
 - Generate random code numbers to mask the identity of the Parts
 - Enable recording the test results without having to "de-randomized" the data



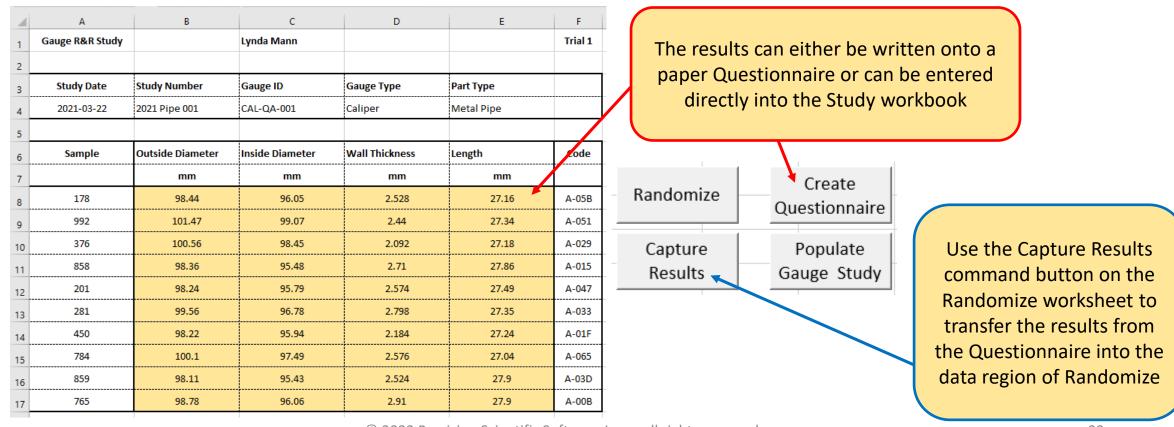
Using the Gauge R & R Template – Randomization

- The randomization table has 1 row for each test that will be performed
 - Rows are grouped by Appraiser and then by Trial (repetition)
 - The Part masking code and order are randomized
 - Up to 4 Characteristics and their specifications can be entered in the template



Using the Gauge R & R Template – Generate Questionnaire

- There are 3 ways to enter the data into the system
 - 1. A Questionnaire worksheet is automatically generated
 - This worksheet can be printed out and each page can be given to an Appraiser
 - Questionnaire includes the random sample codes and space to enter results

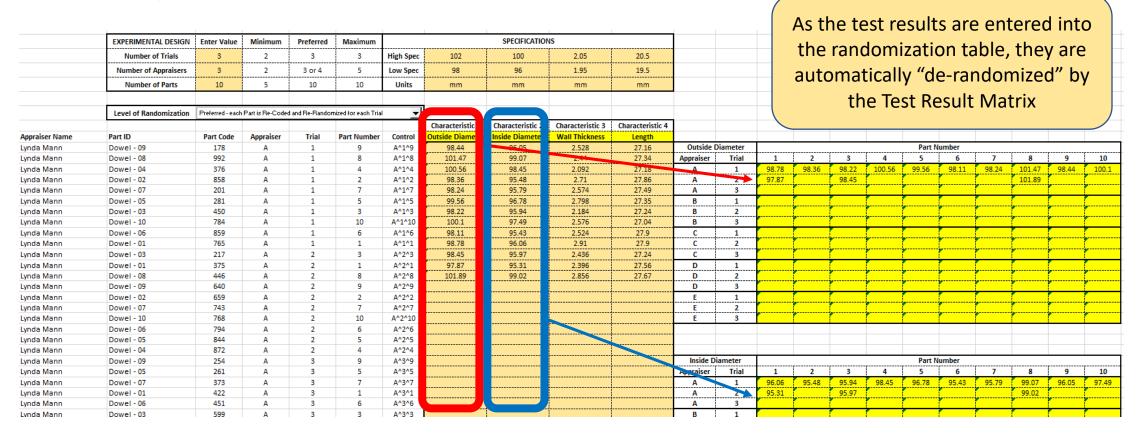


Using the Gauge R & R Template – Enter Data in Randomize

2. If preferred, the results can be entered directly into the data region of the Randomize worksheet

This is especially useful if the Appraisers wrote their results onto paper

Questionnaire sheets



Using the Gauge R & R Template — Populate Gauge Study

 Once all the test results have been entered, use the Populate Gauge Study command button to transfer them from the Test Result Matrix into

the Gauge R & R worksheets

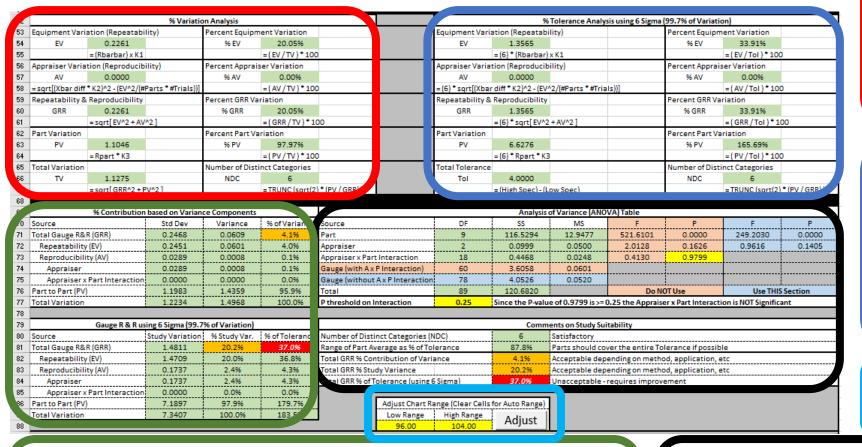
Outside (Diameter		Part Number											
Appraiser	Trial	1	2	2 3		4 5		7	8	9	10			
Α	1	98.78	98.36	98.22	100.56	99.56	98.11	98.24	101.47	98.44	100.1			
Α	2	97.87	98.36	98.45	100.21	99.47	98.23	98.24	101.89	97.8	99.88			
Α	3	97.87	98.21	98.33	100.13	99.69	98.12	98.27	101.31	97.72	99.56			
В	1	98.56	98.13	98.41	100.12	99.47	98.11	98.22	101.36	98.44	100.65			
В	2	98.22	98.36	98.36	100.36	99.89	98.23	98.23	101.47	97.8	99.89			
В	3	98.14	98.34	98.33	100.56	99.78	98.12	98.24	101.87	97.72	100			
С	1	98.56	98.56	98.12	100.25	99.47	98.11	98.27	101.21	98.44	100.12			
С	2	98.22	98.12	98.45	100.36	99.89	98.23	98.26	101.36	97.8	99.25			
С	3	98.15	98.32	98.33	100.22	99.75	98.12	98.22	101.54	97.72	99.69			
D	1													
D	2									Y				

OR:

The results can also be entered directly into the

B B	2	98.22 98.36 98.14 98.4	98.36 98.33	100.36 100.56	99.89 9	98.23 98.23 98.12 98.24	101.47 101.87	97.8 97.72	99.89 100		Gauge R&R worksheets manually							
С	1	98.56 98.56	98.12	100.25	99.47	98.11 98.27	101.21	98.44	100.12	manually								
С	2	98.22 98.12	98.45	100.36		98.23 98.26	101.36	97.8	99.25	Illallually								
С	3	98.15 98.32	98.33	100.22		98.12 98.22			99.69									
D	1																	
D	2							ĺ		Part								
D	3						Part ID	Dowel - 01	Dowel - 02	Dowel - 03	Dowel - 04	Dowel - 05	Dowel - 06	Dowel - 07	Dowel - 08	Dowel - 09	Dowel - 10	
E	1						-	98.78	98.36	98.22	100.56	99.56	98.11	98.24	101.47	98.44	100.10	
E	2				-	Appraiser A Sum	2		98.36	98.45	100.56	99.47		98.24	101.47	97.80	99.88	
E	3					2971.45	3	97.87	98.21	98.33	100.13	99.69	98.12	98.27	101.31	97.72	99.56	
-		1	1	'	+	Sum^2 / Count	Average	98.17	98.31	98.33	100.30	99.57	98.15	98.25	101.56	97.99	99.85	
						Appraiser B	1	98.56	98.13	98.41	100.12	99.47	98.11	98.22	101.36	98.44	100.65	
						Sum	2	98.22	98.36	98.36	100.36	99.89	98.23	98.23	101.47	97.80	99.89	
						2973.38		98.14	98.34	98.33	100.56	99.78	98.12	98.24	101.87	97.72	100.00	
						Sum^2 / Count	Average	98.31	98.28	98.37	100.35	99.71	98.15	98.23	101.57	97.99	100.18	
						Appraiser C	1	98.56	98.56	98.12	100.25	99.47	98.11	98.27	101.21	98.44	100.12	
						Sum	2		98.12	98.45		99.89	98.23			97.80	99.25	
						2971.11					100.22						99.69	
						Sum^2 / Count	Average	98.31	98.33	98.30	100.28	99.70	98.15	98.25	101.37	97.99	99.69	
						=					1				-	_	_	
						Appraiser D	11			 			-					

Using the Gauge R & R Template – Report



% Variation Analysis

Calculates the Study's Actual and Percent EV (Repeatability), AV (Reproducibility), GRR, PV (Part Variation), and TV (Total Variation)

Also calculates the NDC

% Tolerance Analysis

Using either 5.15 σ or 6 σ (99% or 99.7% of the Variation)

Use 6 σ for critical applications such as Automotive. The less rigorous 5.15 σ can be used if desired for other applications.

Adjust Chart Range
Use to set the Chart Ranges if the
Excel defaults are not suitable

% Contribution of Variance Components and Gauge R & R Components

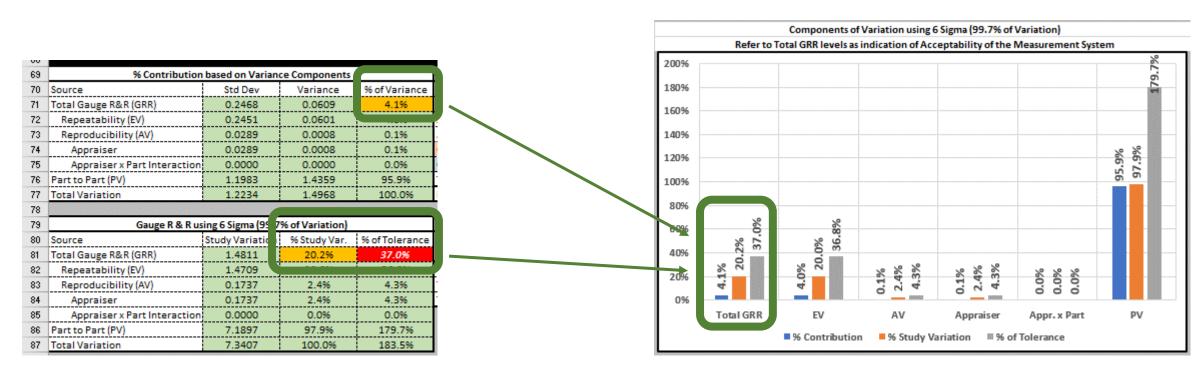
This shows the contribution of each of the components to the Total Variation. Most importantly, it shows the GRR as a percent of the Variance, of the Study Variance, and of the Tolerance (note the cells highlighted in orange and red).

ANOVA Table and Comments on Study Suitability

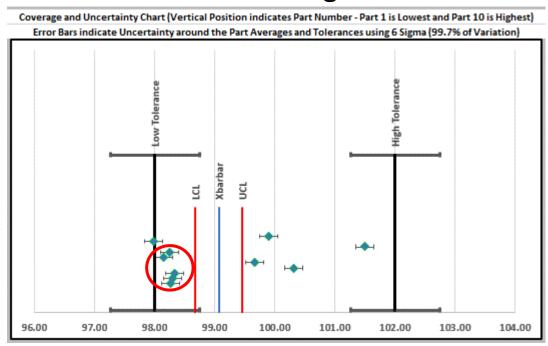
The ANOVA Table shows the F and P-values for the Part, Appraiser, and Appraiser x Part Interaction. A P-value less than 0.05 shows a statistically significant relationship.

The Study Suitability shows the commentary on the NDC and the GRR.

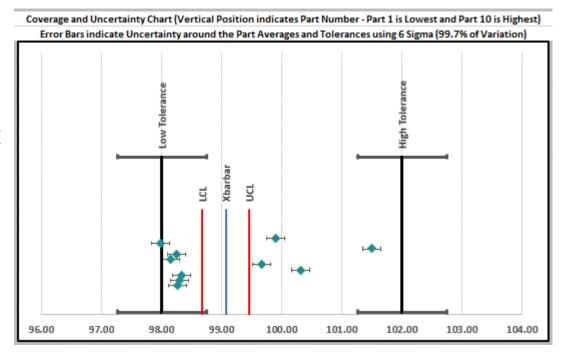
- Components of Variation Chart
 - This chart graphs the breakdown of the components of the Gauge R & R Study the % Contribution, % Study Variation, and % of Tolerance
 - The most critical factors are the Total GRR component which is the sum of the Repeatability and Reproducibility



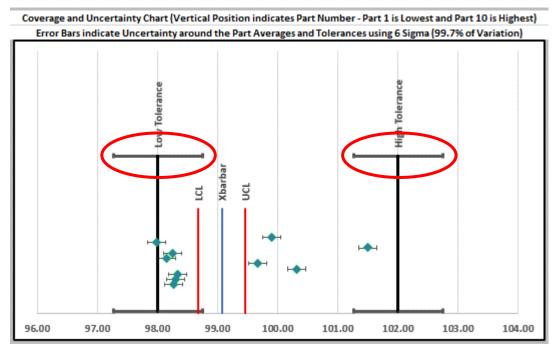
- Coverage and Uncertainty Chart Parts Measurements
 - The measurement is shown on the horizontal scale at the bottom
 - The green points are the average measurements for each Part
 - The vertical height of each point indicates the Part number
 - Part 1 is the lowest point and Part 10 is the highest
 - The error bars indicate the 95% confidence limits around the averages
- Number of Distinct Categories (NDC)
 - Each distinct category comprises those Parts that cannot be statistically distinguished from each other
 - This plot shows 6 groups of Parts whose error bars overlap each others' averages
 - Parts 1, 2, 3, 6, and 7 cannot be distinguished so they comprise 1 DC



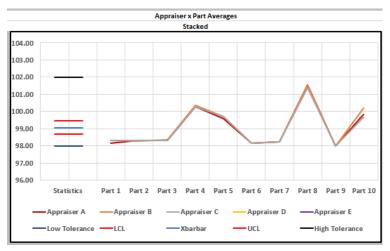
- Coverage and Uncertainty Chart Average and Confidence Limits
 - $ar{ar{X}}$ (Xbarbar) is the overall average
 - LCL and UCL are the control limits around the overall average
 - Note that the Part measurements are outside the control limits
 - This is good: the control limits are based on the GRR calculations
 - By being outside the control limits, the measurements indicate that most of the variation is due to Part-to-Part (process) rather than Gauge (measurement) variation

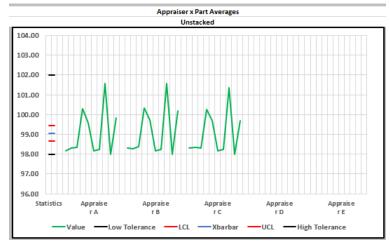


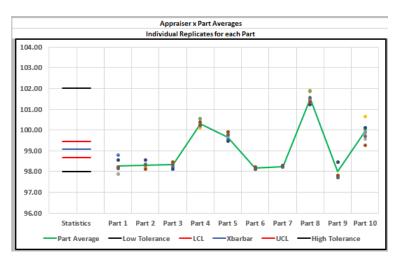
- Coverage and Uncertainty Chart Tolerances
 - The Low and High Tolerances (98 mm to 102 mm) are shown
 - Error bars on the Tolerance show the width of the GRR relative to the Tolerance
 - Any measurement within these error bars may be in or out of the Tolerance
 - Example: the Tolerance has a width of 4 mm and the GRR is 37% of that width
 - 37% of 4 mm is 1.48 mm (± 0.74 mm)
 - At the low end the uncertainty goes from 97.26 mm to 98.74 mm
 - 101.26 to 102.74 mm at the high end
 - You cannot be certain whether any measurement in this range indicates that the Part is in or out of spec
 - If the GRR encompasses too much of the Tolerance then the process cannot be monitored for on-spec performance



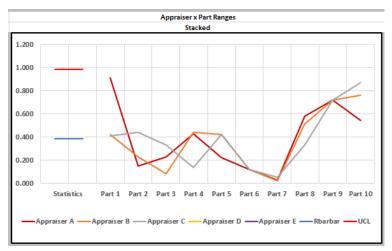
- Appraiser x Part Average Charts
 - These charts show 3 views of the same information
 - Average measurements for all parts as measured by each appraiser
 - 1. All appraisers overlapped to show any differences between appraisers
 - 2. All appraisers individually to more clearly compare their patterns
 - 3. Average and individual measurements for each part
 - Short bars at the right show the Tolerances, Control Limits, and Overall Average

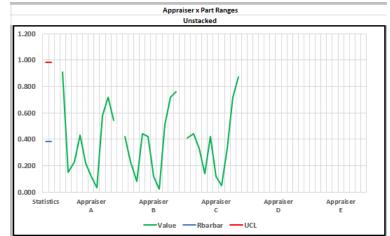


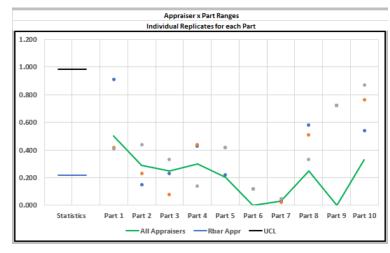




- Appraiser x Part Range Charts
 - These charts show 3 views of the same information
 - Range measurements for all parts as measured by each appraiser
 - 1. All appraisers overlapped to show any differences between appraisers
 - 2. All appraisers individually to more clearly compare their patterns
 - 3. Range and individual measurements for each part
 - Short bars at the right show the Upper Control Limit and Overall Average
 - The Range does not have Tolerances and the Lower Control Limit on Range is 0





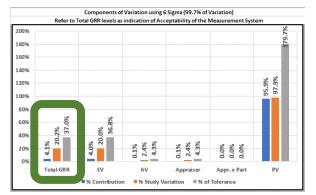


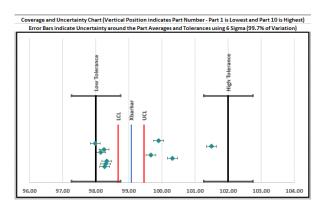
Recap of Gauge R & R – Summary of Key Points

- Gauge R & R is an analysis of the repeatability and reproducibility of the Measurement System – it is not an analysis of the product
- Experimental Design
 - Set the appropriate level of Coverage of Variation
 - 6 σ for critical applications (eg automotive) or 5.15 σ for less rigor
 - Use at least 2 (preferably 3 or 4) appraisers to measure up to 10 parts
 - At least 2 (preferably 3) repetitions per part
 - Randomize and mask the parts to avoid subjective bias
 - The parts should cover the entire range of the product's tolerance
 - The Number of Distinct Categories (NDC) should be at least 5

Recap of Gauge R & R – Summary of Key Points

- Determine the acceptability of the measurement system
 - Does the GRR meet the recommended standards of acceptability?
 - % Contribution to Variance: < 1% (< 9% depending on application)
 - % Study Variation & % of Tolerance: < 10% (< 30% depending on application)
 - If the GRR is > 30% of the width of the Tolerance then there is too much uncertainty in the identification of in-spec or out-of-spec parts
- Review all report statistics and charts
 - The most informative charts are:
 - Components of Variation
 - Coverage and Uncertainty





• If GRR is not acceptable, possible remedies are appraiser training, equipment calibration / maintenance, or upgrading the test equipment